

Effect of unitarity on three-pions decay of heavy meson resonances

Satoshi Nakamura

Excited Baryon Analysis Center (EBAC), JLab

EBAC Collaborators

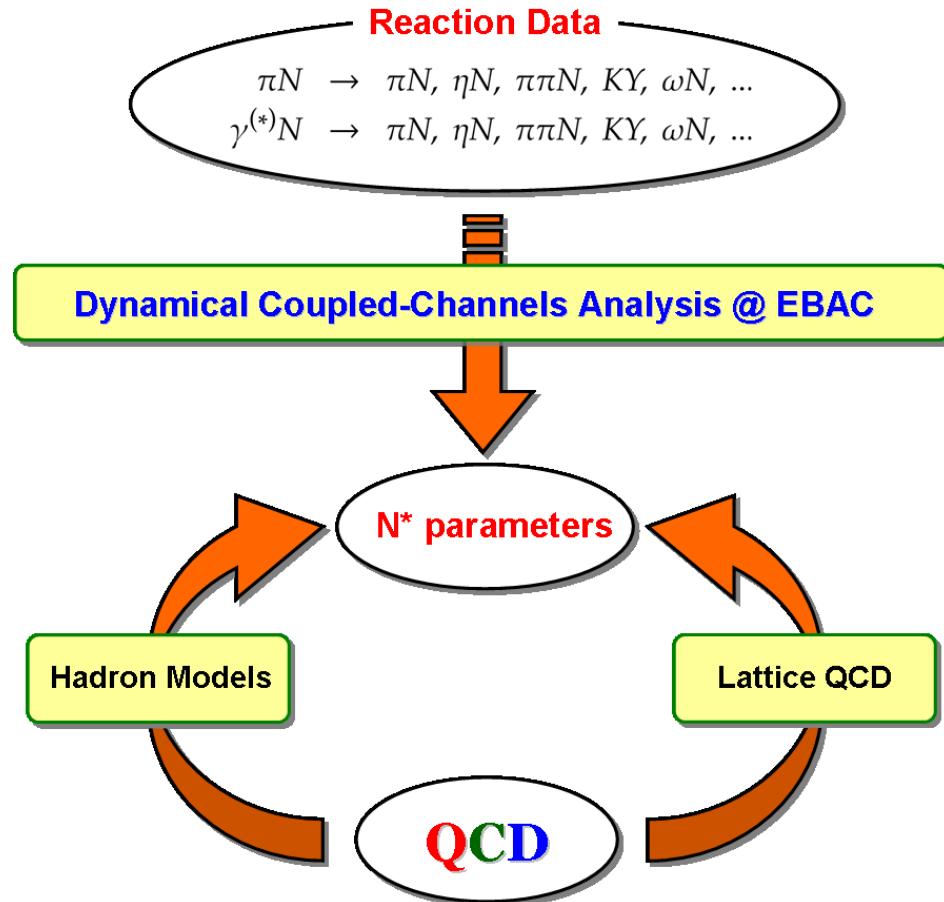
Hiroyuki Kamano (JLab)

Harry Lee (ANL)

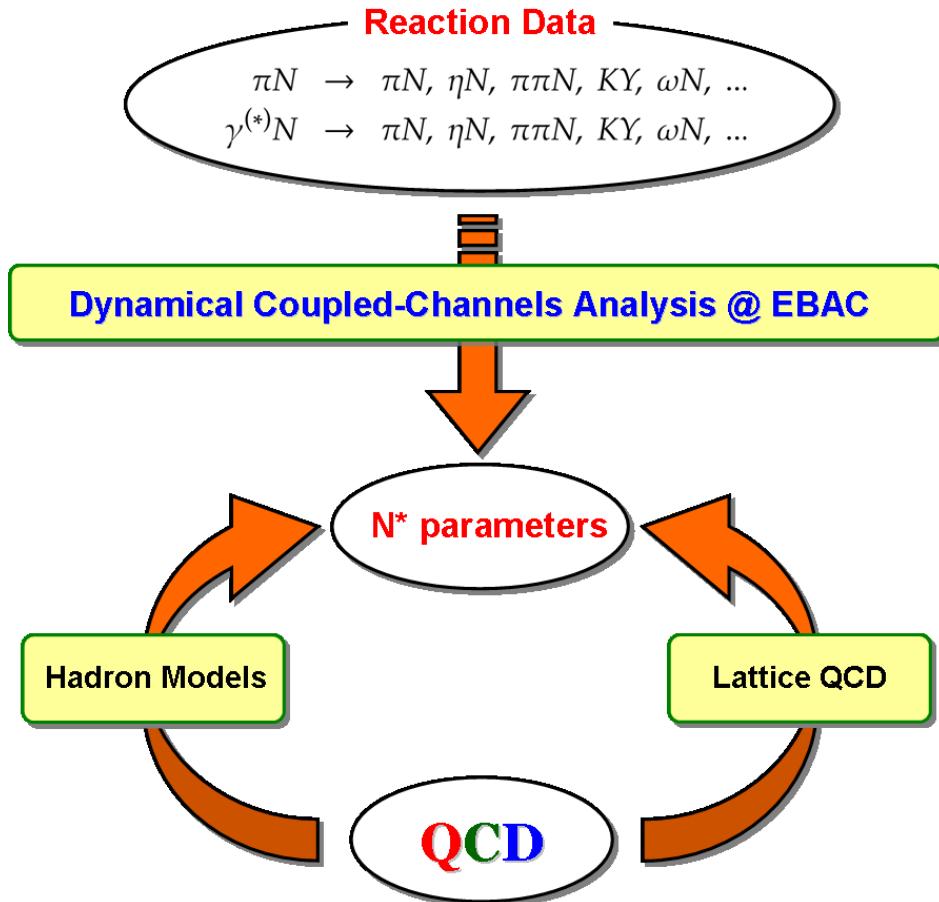
Toru Sato (Osaka Univ.)

Summary of recent EBAC activity on N^*

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Strategy Step 1

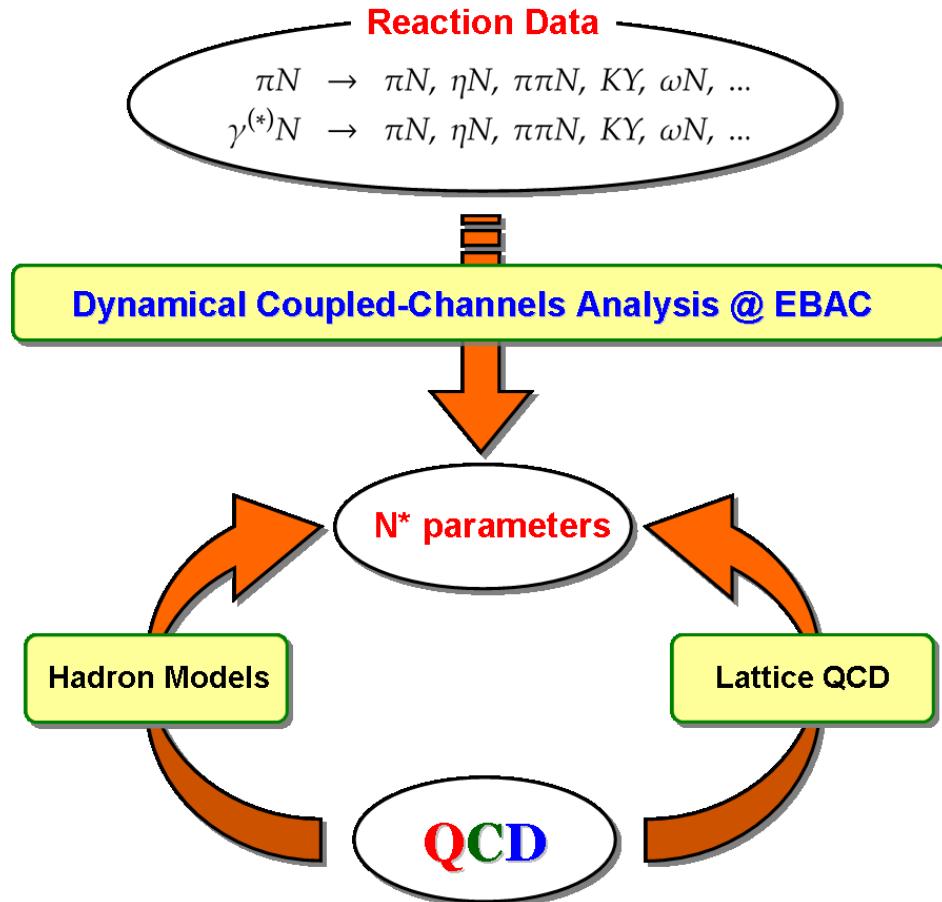
Comprehensive Dynamical
Coupled-channels (DCC) analysis of
 $\pi N, \gamma N, N(e, e')$ reactions data

EBAC's DCC model

Matsuyama et al., Phys. Rep. **439**, 193 (2007)

DCC model provides
reaction mechanism for interpreting
N* structure, dynamical origin

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Strategy Step 2

Extract N^* from DCC model

* N^* pole positions

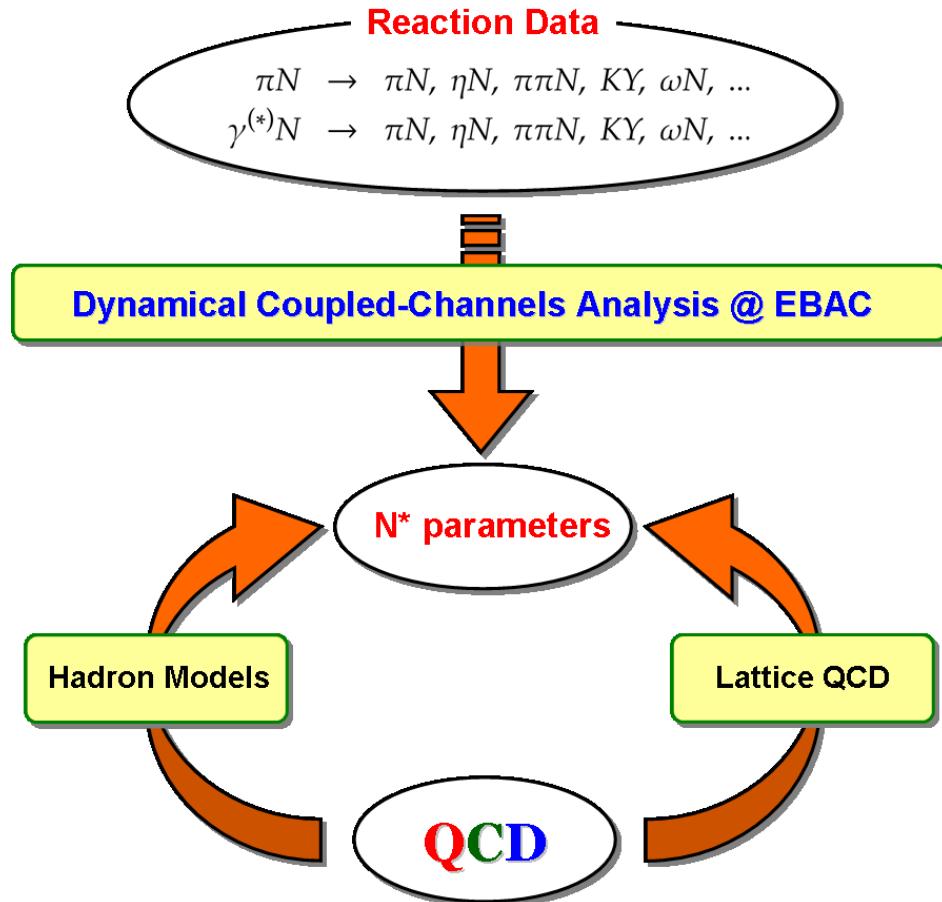
$N^* \rightarrow \gamma N, MB$ form factors

* confirm or reject low-star N^*
search for new N^*

Analytic continuation of amplitudes
to complex energy plane

Suzuki et al., PRC 79 025205; ibid, 82 045206

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Strategy Step 3

Make a connection between
extracted N^* to
hadron structure calculation

- * Quark model
- * Dyson-Schwinger equation
- * Lattice QCD

EBAC's DCC (Dynamical Coupled-Channel) model

Matsuyama et al., Phys. Rep. **439**, 193 (2007)

Lippmann-Schwinger equation

$$T_{ab} = V_{ab} + \sum_c V_{ac} G_c T_{cb}$$
$$V_{ab} = v_{ab} + \sum_{N^*} \frac{\Gamma_{N^*,a}^\dagger \Gamma_{N^*,b}}{E - m_{N^*}^0}$$

exchange-potentials bare N* terms

$$\{a, b, c\} = \gamma^{(*)} N, \pi N, \eta N, \pi\pi N(\pi\Delta, \sigma N, \rho N)$$

EBAC's DCC (Dynamical Coupled-Channel) model

Matsuyama et al., Phys. Rep. **439**, 193 (2007)

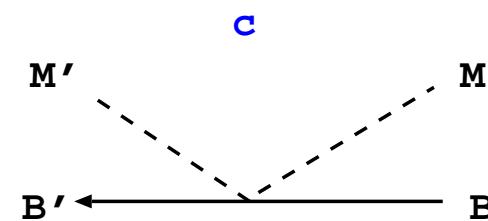
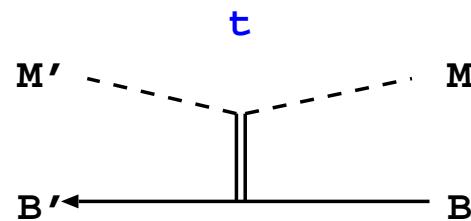
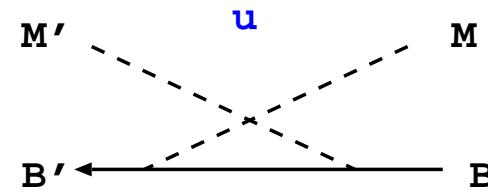
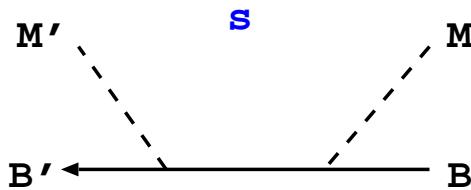
Lippmann-Schwinger equation

$$T_{ab} = V_{ab} + \sum_c V_{ac} G_c T_{cb}$$
$$V_{ab} = v_{ab} + \sum_{N^*} \frac{\Gamma_{N^*,a}^\dagger \Gamma_{N^*,b}}{E - m_{N^*}^0}$$

exchange-potentials bare N* terms

$$\{a, b, c\} = \gamma^{(*)} N, \pi N, \eta N, \pi\pi N(\pi\Delta, \sigma N, \rho N)$$
$$K\Lambda, K\Sigma, (\omega N)$$

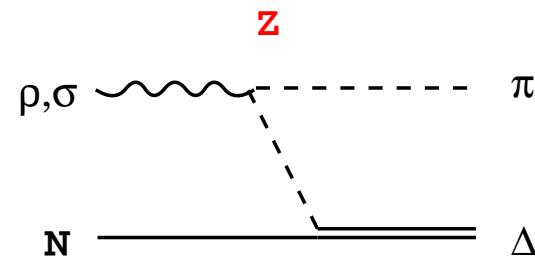
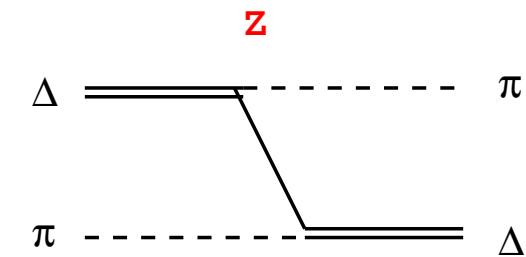
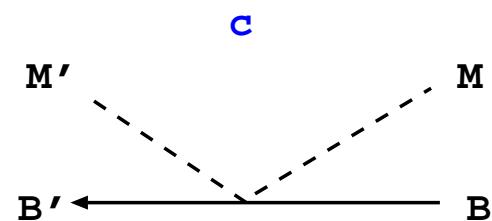
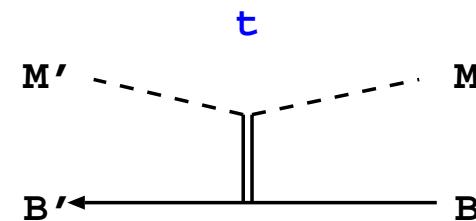
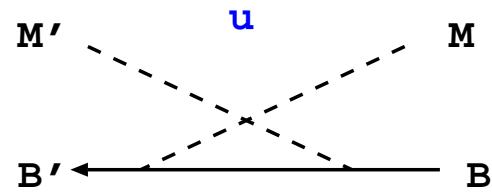
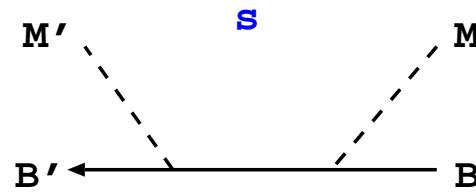
Meson-exchange potentials (v_{ab}) for πN scattering



$$B, B' = N, \Delta, Y$$

$$M, M' = \pi, \eta, \rho, \sigma, K$$

Meson-exchange potentials (v_{ab}) for πN scattering



Achievements so far (2006–2009)

- * $\pi N \rightarrow \pi N$ fitted up to 2 GeV PRC76 065201 (2007)
- * $\pi N \rightarrow \pi\pi N$ up to 2 GeV PRC79 025206 (2009)
- * $\pi N \rightarrow \eta N$ fitted up to 2 GeV PRC78 025204 (2008)
- * $\gamma N \rightarrow \pi N$ fitted up to 1.6 GeV PRC77 045205 (2008)
- * $N(e, e'\pi)$ fitted up to $Q^2 = 1.5$ GeV² PRC80 025207 (2009)
- * $\gamma N \rightarrow \pi\pi N$ up to 1.6 GeV PRC80 065203 (2009)
- * Extraction of N^* properties PRL104 065203 (2010), PRC82 045206 (2010)

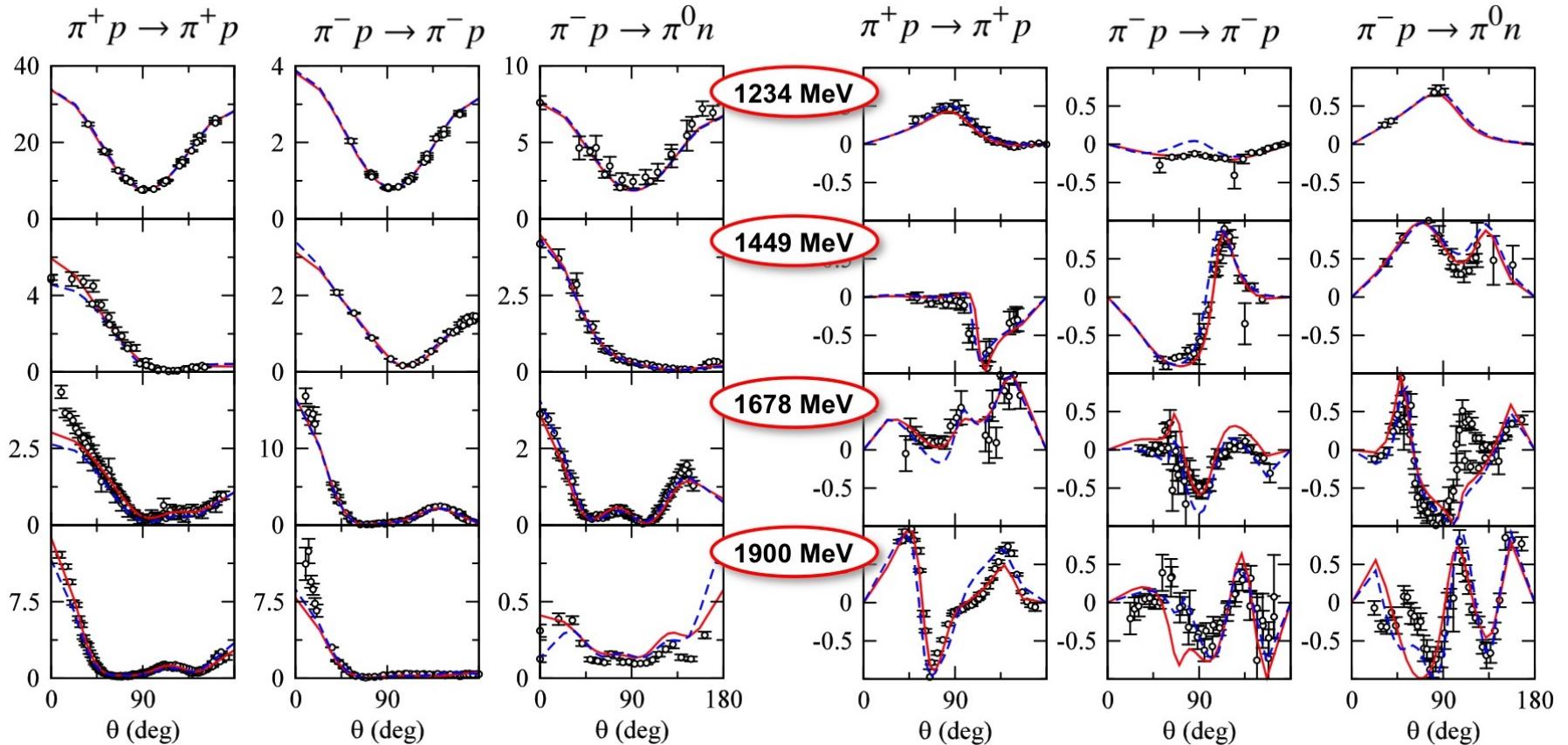
EBAC-DCC Analysis since 2010

	2006 – 2009	2010 ~
# of coupled-channels	$\overset{5}{(\pi N, \eta N, \pi\Delta, \sigma N, \rho N)}$	$\overset{7}{(\pi N, \eta N, \pi\Delta, \sigma N, \rho N, K\Lambda, K\Sigma)}$
* $\pi N \rightarrow \pi N$	$< 2 \text{ GeV}$	$< 2 \text{ GeV}$
* $\gamma N \rightarrow \pi N$	$< 1.6 \text{ GeV}$	$< 2 \text{ GeV}$
* $\pi N \rightarrow \eta N$	$< 2 \text{ GeV}$	$< 2 \text{ GeV}$
* $\gamma N \rightarrow \eta N$	–	$< 2 \text{ GeV}$
* $\pi N \rightarrow KY$	–	$< 2.1 \text{ GeV}$
* $\gamma N \rightarrow K\Lambda$	–	$< 2.1 \text{ GeV}$



Fully-combined Analysis of $\pi N, \gamma N \rightarrow \pi N, \eta N, KY (\omega N)$!

$\pi N \rightarrow \pi N$ (preliminary)



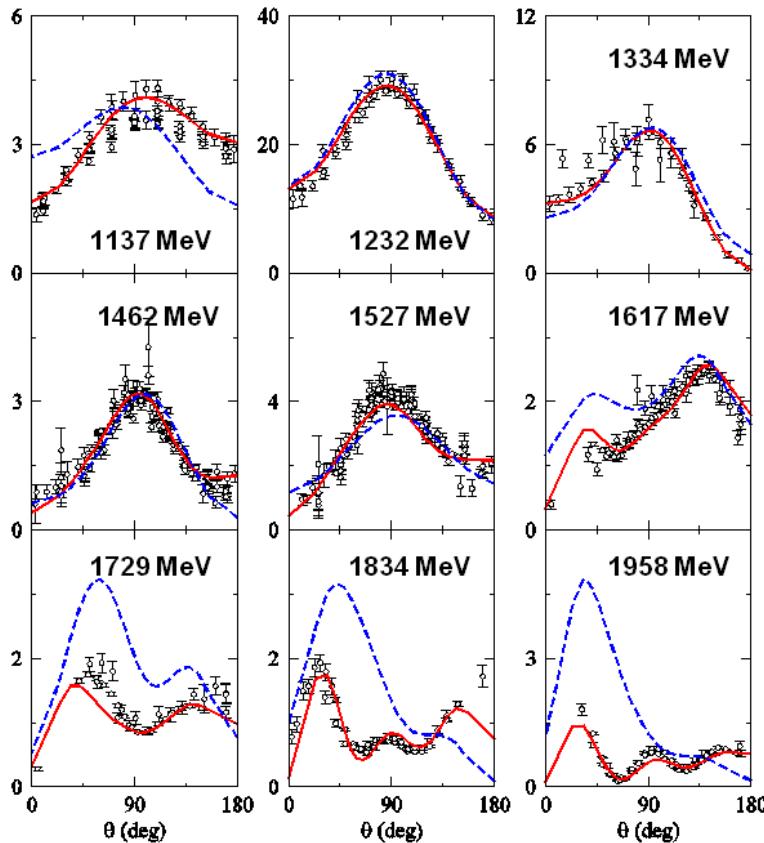
red: Current full-combined analysis

blue dashed: Previous model [PRC76, 065201 (2007)] fitted to $\pi N \rightarrow \pi N$ data only

$\gamma p \rightarrow \pi^0 p$ (preliminary)

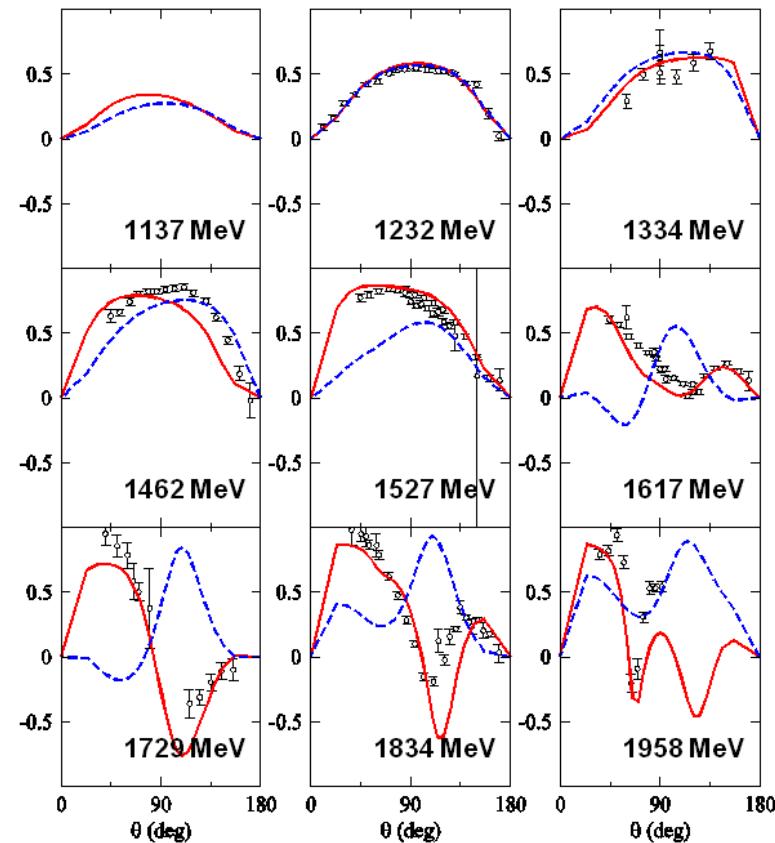
Angular distribution

$d\sigma/d\Omega$ ($\mu\text{b}/\text{sr}$)



Photon asymmetry

Σ

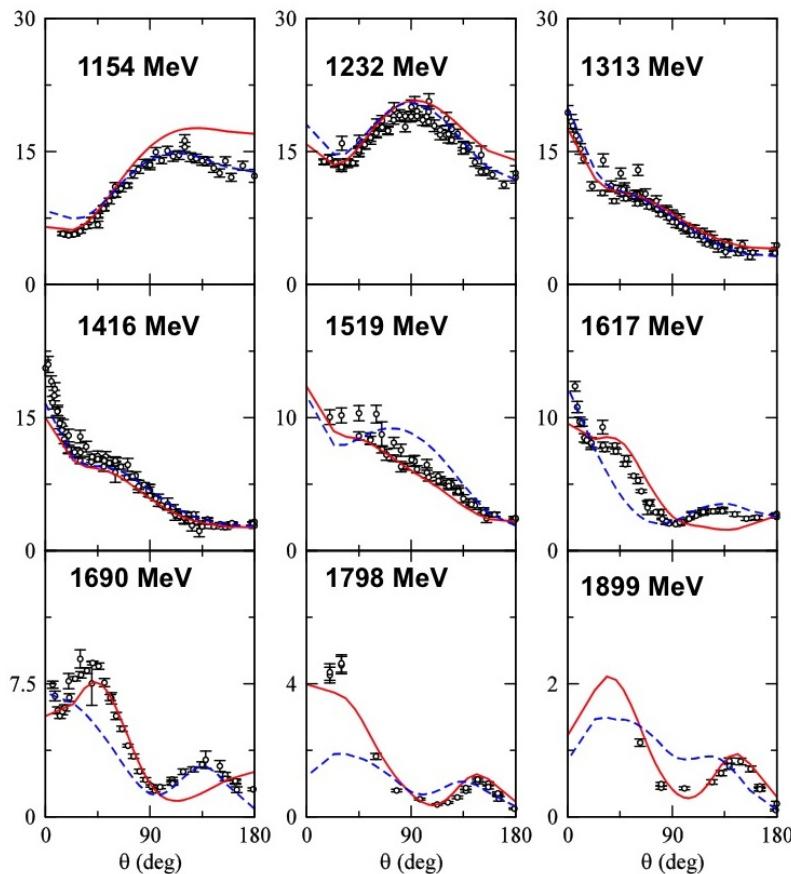


red: Current **full-combined** analysis

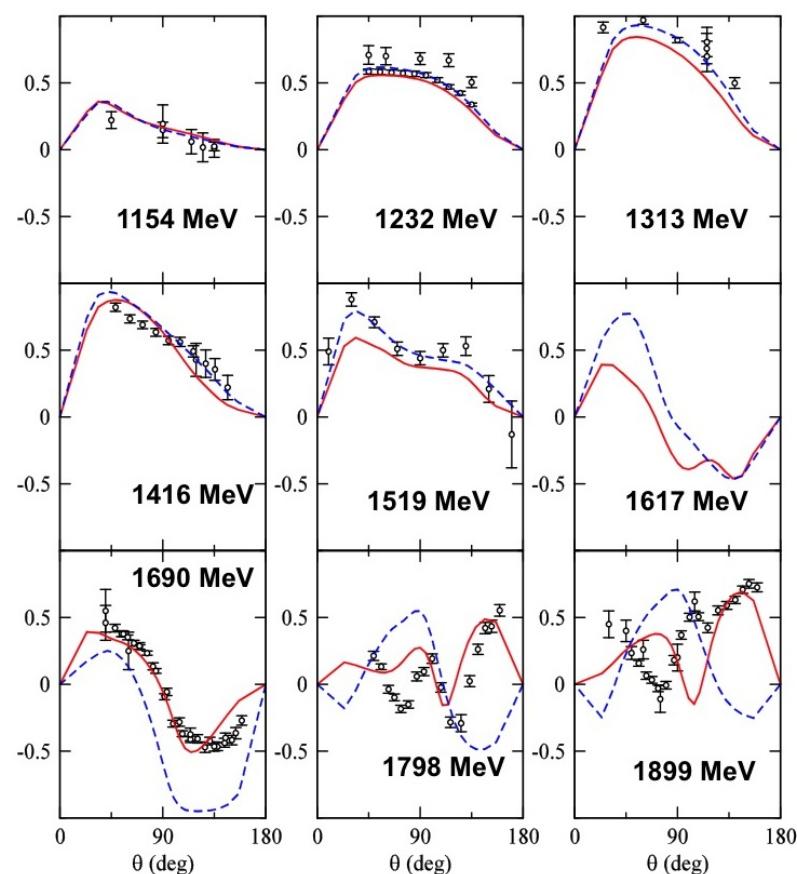
blue dashed: Previous model [PRC77, 045205 (2008)] fitted to $\gamma N \rightarrow \pi N$ data up to 1.6 GeV

$\gamma p \rightarrow \pi^+ n$ (preliminary)

Angular distribution $d\sigma/d\Omega$ ($\mu\text{b}/\text{sr}$)



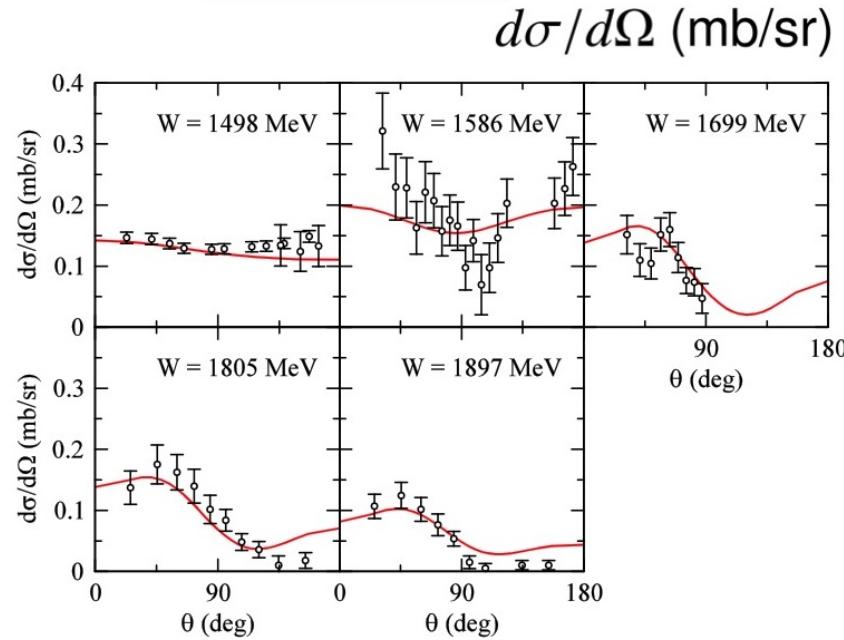
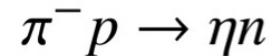
Photon asymmetry Σ



red: Current **full-combined** analysis

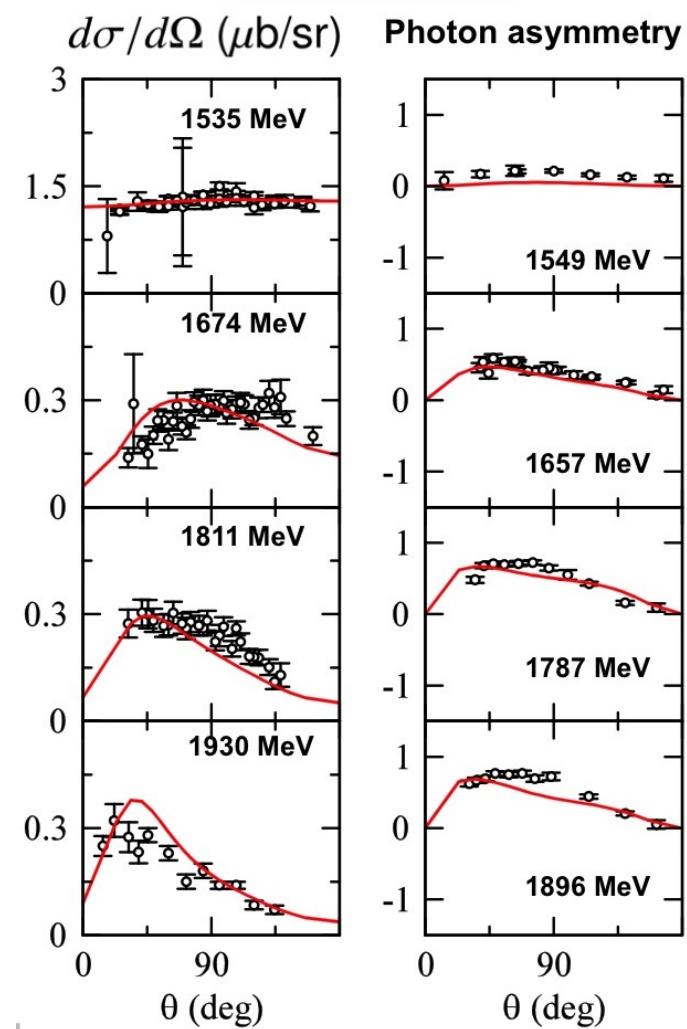
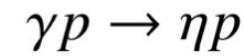
blue dashed: Previous model [PRC77, 045205 (2008)] fitted to $\gamma N \rightarrow \pi N$ data up to 1.6 GeV

η productions (preliminary)



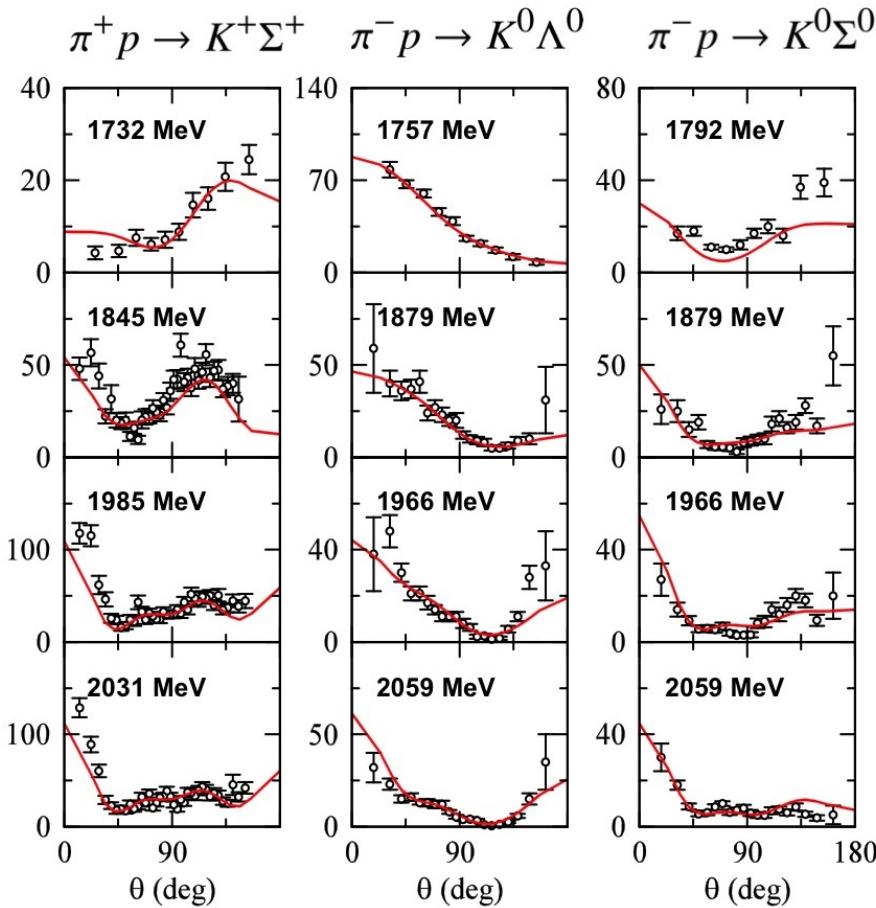
Data are selected following
Durand et al. PRC78 025204

Analyzed data up to $W = 2$ GeV

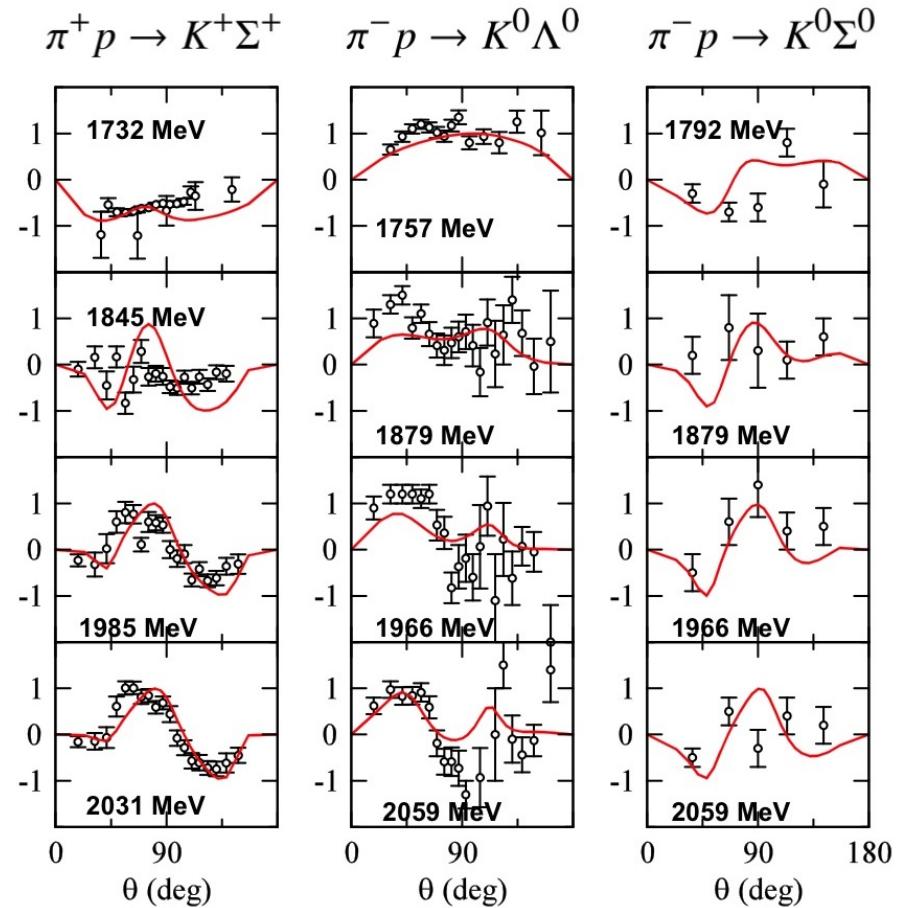


$\pi N \rightarrow KY$ (preliminary)

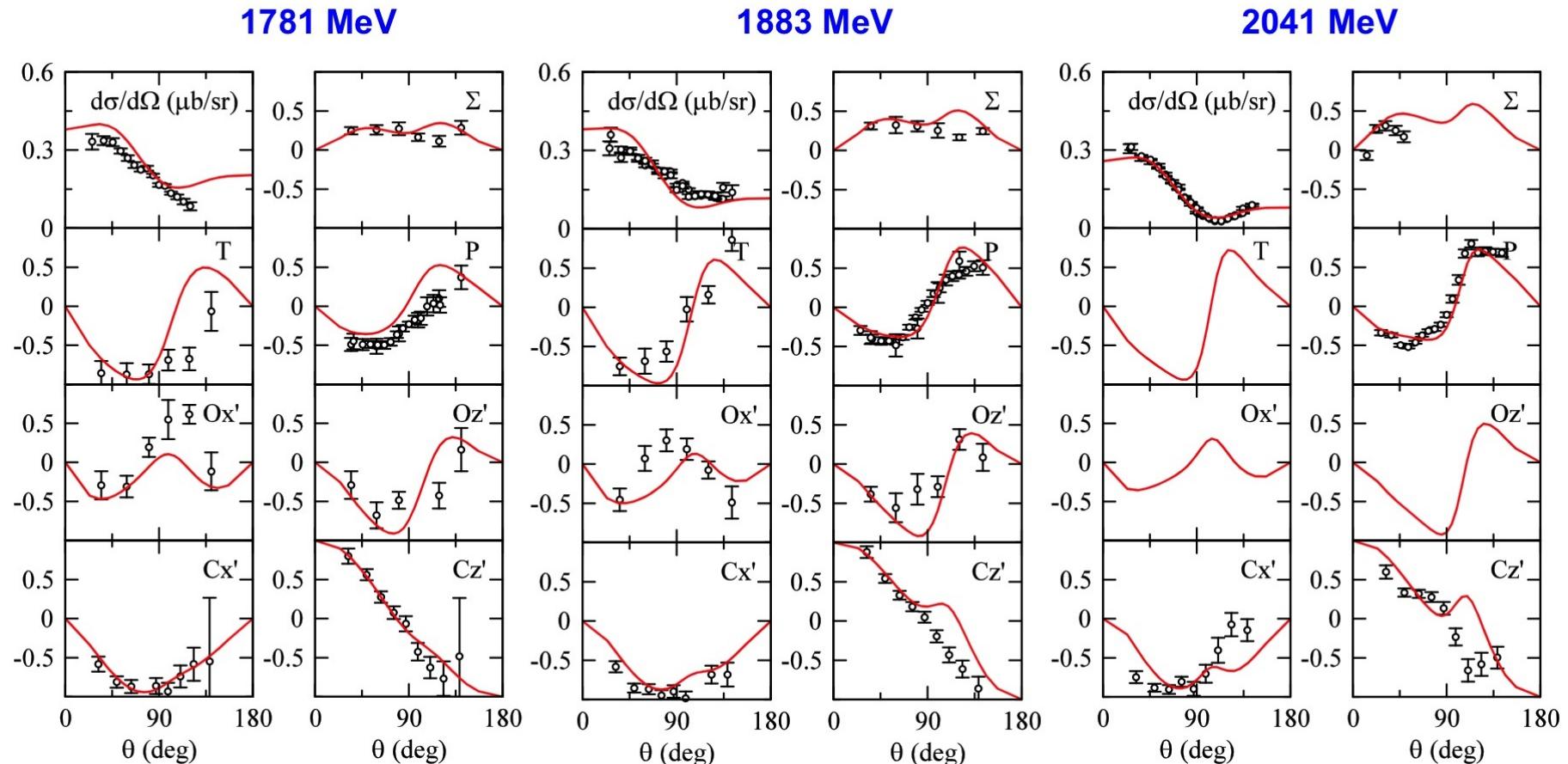
Angular distribution $d\sigma/d\Omega$ ($\mu\text{b}/\text{sr}$)



Recoil polarization



$\gamma p \rightarrow K^+ \Lambda$ (preliminary)



Over-complete experiment is planned by CLAS@JLAB

⇒ New N^* states !

Effect of unitarity on three-pions decay of heavy meson resonances

Introduction

Why we care 3π ($\pi\pi K$, etc.) scattering ?

Introduction

Why we care 3π ($\pi\pi K$, etc.) scattering ?

⇒ Information of interesting physics is hidden in 3π from heavy meson decays

e.g.,

- * Exotic (hybrid) mesons (e.g., $J^{PC} = 1^{-+}$) BNL(E852), JLab(GlueX, CLAS12)

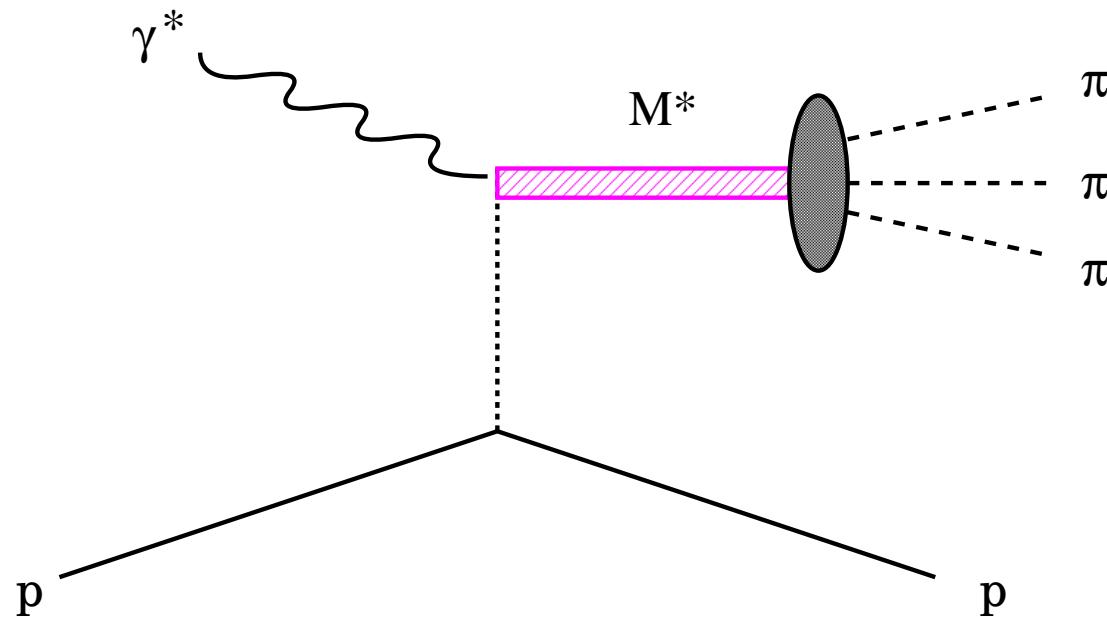
⇒ Gluon self interaction

- * CP-violation from B- and D-decays BABAR, Belle

⇒ CKM matrix, beyond SM contribution

GlueX, CLAS12 experiment

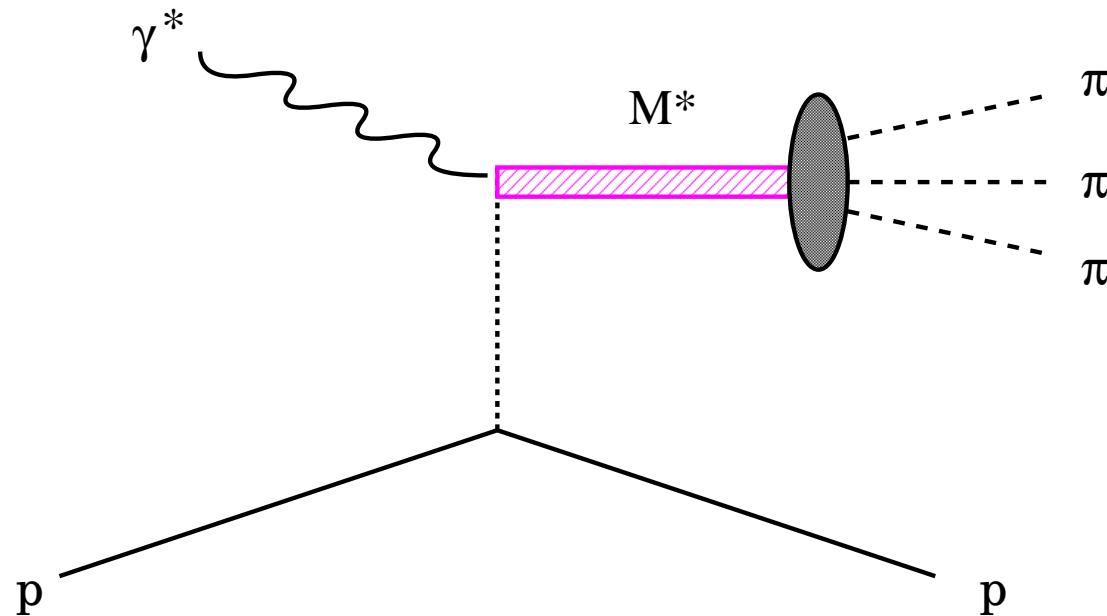
(JLab, planned after 12 GeV upgrade)



New EBAC project : Analysis of 3π FSI in heavy meson decays

GlueX, CLAS12 experiment

(JLab, planned after 12 GeV upgrade)



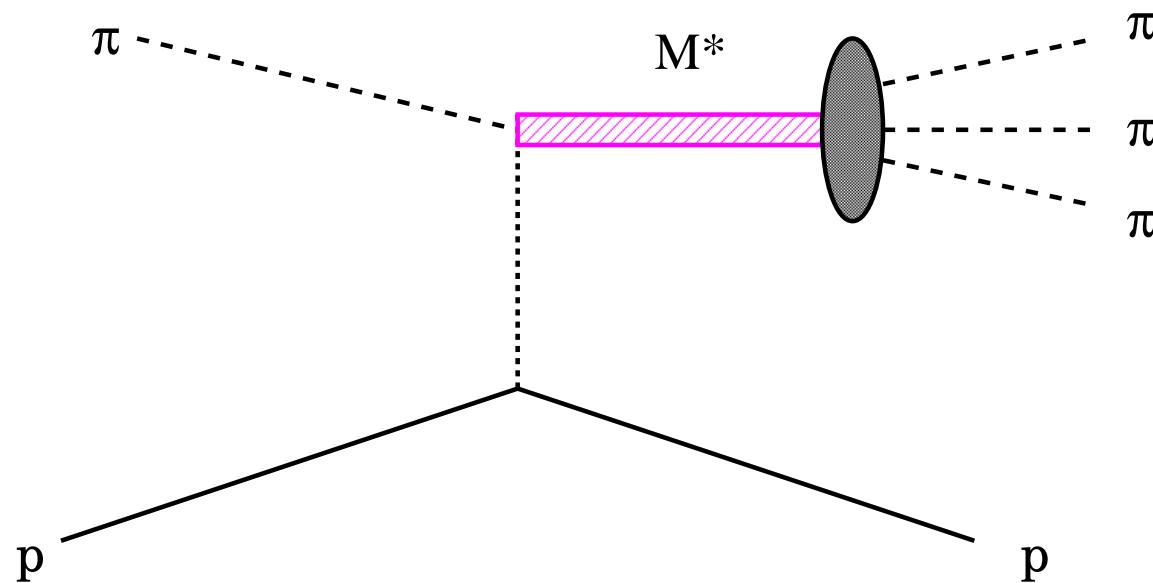
EBAC —> EHAC ?

(Excited Hadron Analysis Center)

Previous analysis of 3π decay of M^*

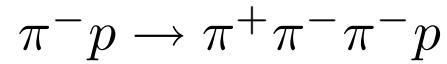
E852 (BNL) $\pi^- p \rightarrow \pi^+ \pi^- \pi^- p$

Chung et al., PRD **65**, 072001 (2001)

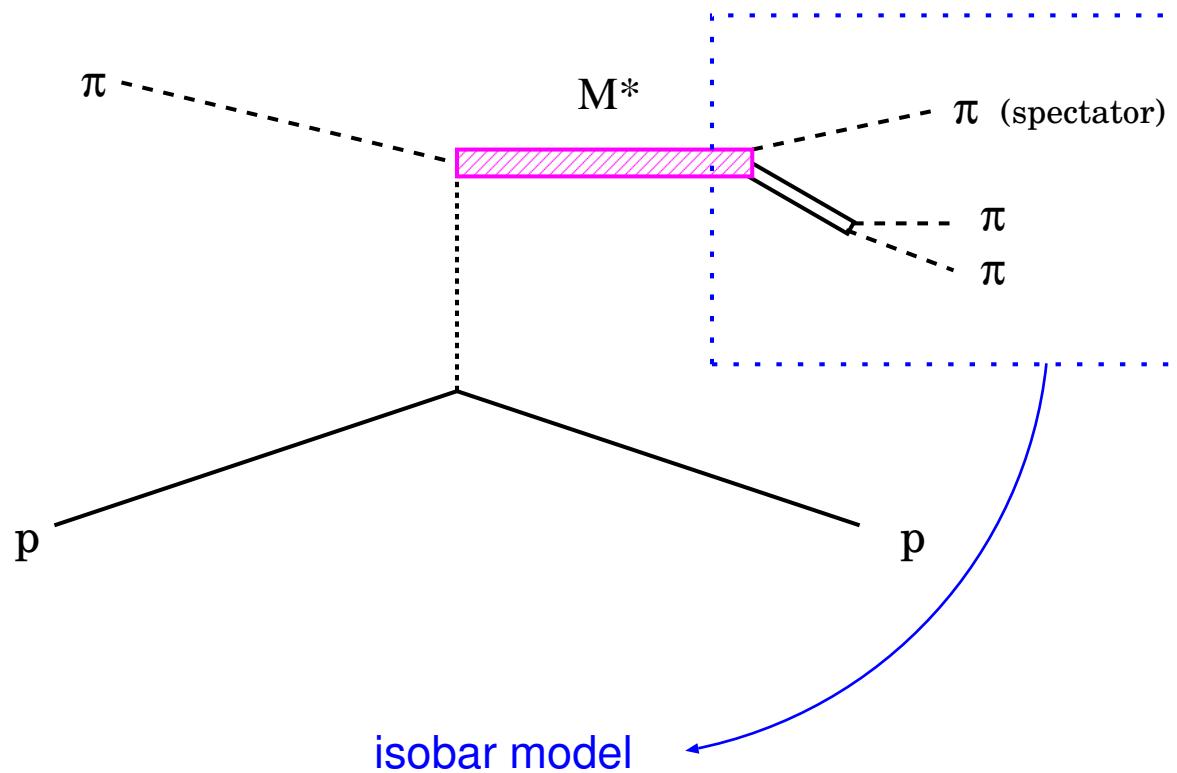


Previous analysis of 3π decay of M^*

E852 (BNL)



Chung et al., PRD **65**, 072001 (2001)



* $\pi\pi$ subsystem forms a resonance

* 3rd π is a spectator (3 π unitarity missing !)

Our objective

(This work)

Examine **the effect of 3π unitarity** on

- * **Pole position** of heavy meson resonance
- * **Dalitz plot** of heavy meson 3π decay

⇒ address the basic assumption of the isobar model

(Long term)

Comprehensive development of reliable 3π ($\pi\pi K$ etc.) model

Coupled-Channels Model

Matsuyama, Sato, Lee, Phys. Rept. **439**, 193 (2007)

$$M^* \rightarrow \pi R_{\pi\pi} \text{ (or } \bar{K} R_{\pi K}) \rightarrow \pi\pi\pi$$

Channels $R_{\pi\pi}$: $f_0(600), f_0(980), \rho(760), f_2(1270)$

$R_{\pi K}$: $K_0^*(800), K_0^*(1430), K^*(892), K^*(1680)$

$R_{\pi\pi}$ ($R_{\pi K}$): resonance in $\pi\pi$ (πK) scattering

- (I) Develop $\pi\pi$ (πK) model
- (II) Develop $\pi R_{\pi\pi}$ ($\bar{K} R_{\pi K}$) interaction
- (III) Solve $\pi R_{\pi\pi}$ ($\bar{K} R_{\pi K}$) scattering equation

Simple $\pi\pi$ model

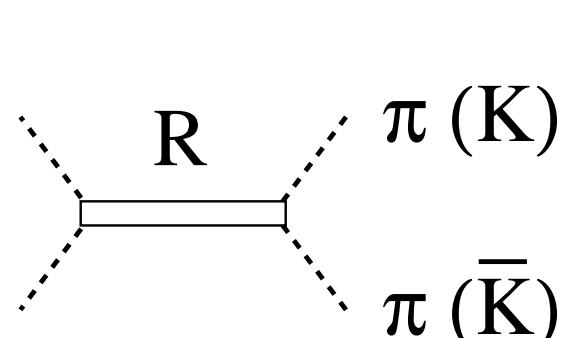
Coupled-channel scattering equation for $\pi\pi$ partial wave (L, I)

$$t_{i,j}^{LI}(p', p; W) = V_{i,j}^{LI} + \sum_k \int_0^\infty q^2 dq V_{i,k}^{LI}(p', q; W) \frac{1}{W - E_k(q) + i\epsilon} t_{k,j}^{LI}(q, p; W)$$

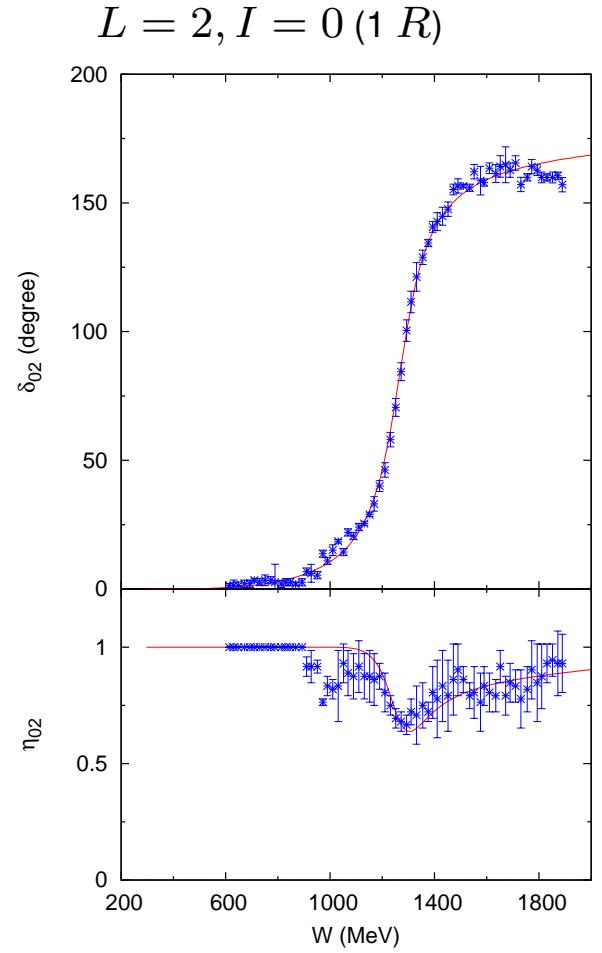
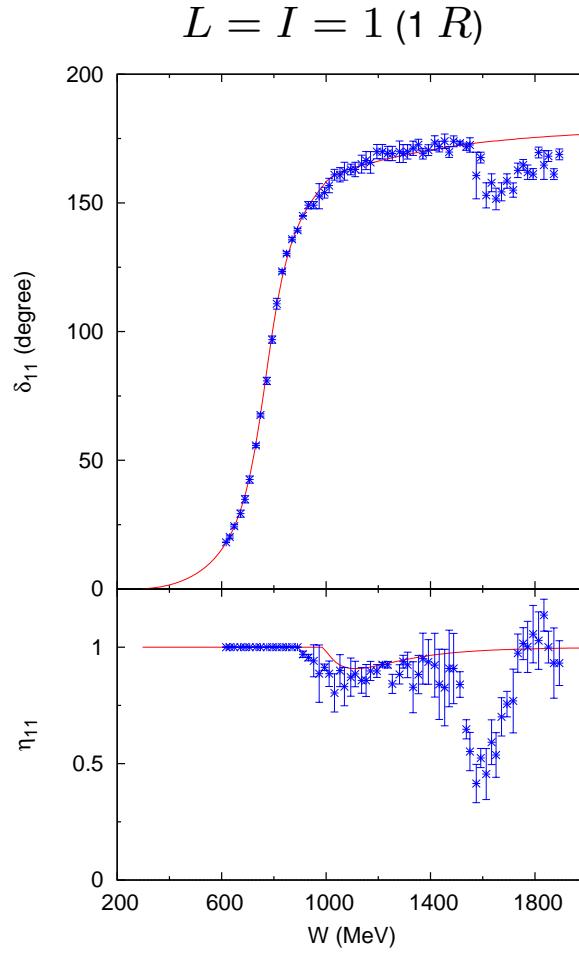
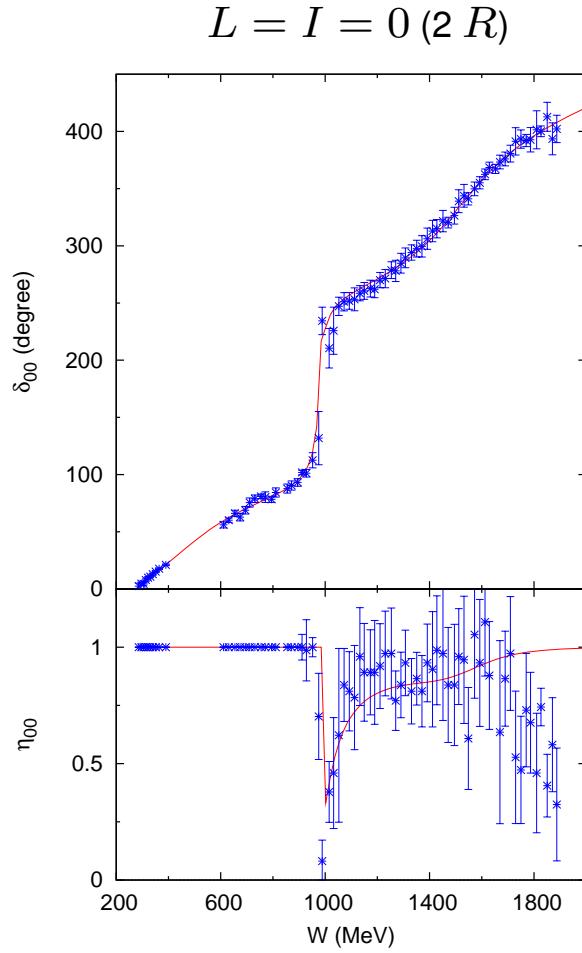
$$E_{\pi\pi}(q) = 2\sqrt{m_\pi^2 + q^2} \quad (i, j, k = \pi\pi, K\bar{K})$$

$$V_{i,j}^{LI}(p', p; W) = \sum_R f_{R,i}^{LI}(p') \frac{1}{W - m_R} f_{R,j}^{LI}(p)$$

$$f_{R,i}^{LI}(p) = \frac{g_{R,i}}{\sqrt{m_\pi}} \frac{1}{(1 + (c_{R,i} p)^2)} \left(\frac{p}{m_\pi} \right)^L$$



Phase and inelasticity of $\pi\pi$ amplitude



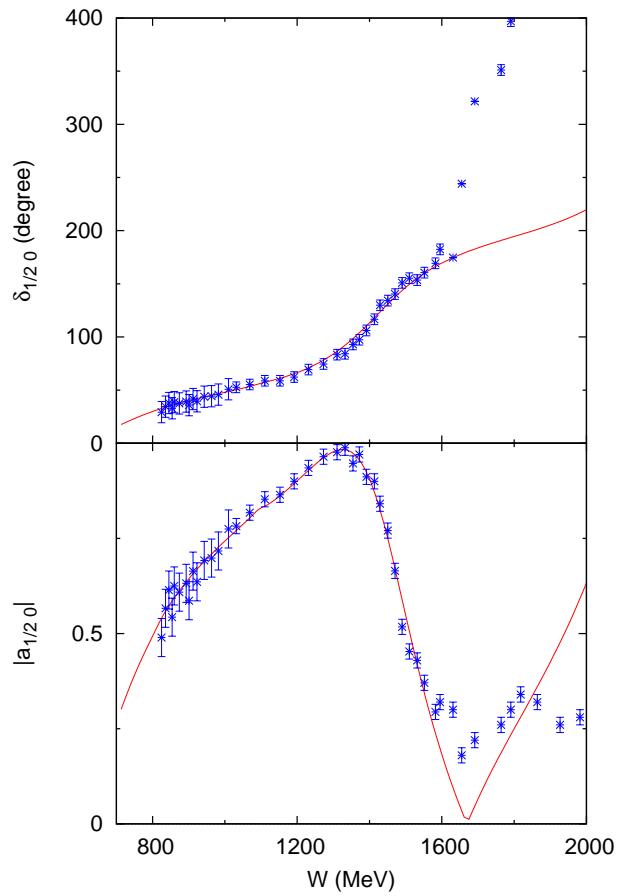
[Data: G. Gayer et al., NPB **75**, 189 (1974)]

Pole positions in $\pi\pi$ amplitude

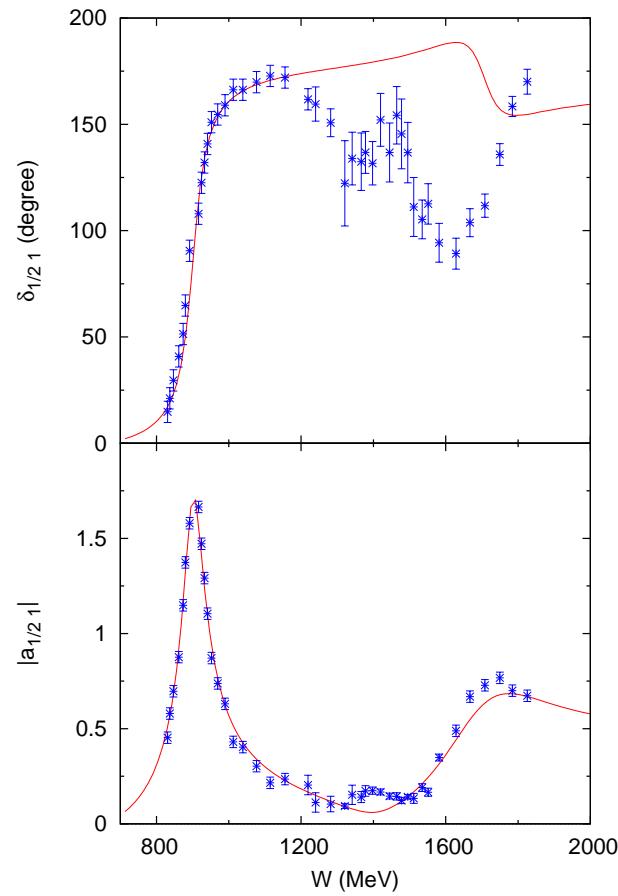
	Re[M_R] (MeV)		−Im[M_R] (MeV)	
	Ours	PDG	Ours	PDG
f_0 (600)	437	400 – 1200	256	300 – 500
f_0 (980)	897	980 ± 10	69	20 – 50
f_0 (1500)	1527	1505 ± 6	237	54.5 ± 3
ρ (760)	769	775.5 ± 0.3	81	74.5 ± 0.4
f_2 (1270)	1249	1275 ± 1.2	101	92.5 ± 1.3

Phase and magnitude of πK amplitude

$L = 0, I = 1/2$ ($2 R$)



$L = I, I = 1/2$ ($2 R$)

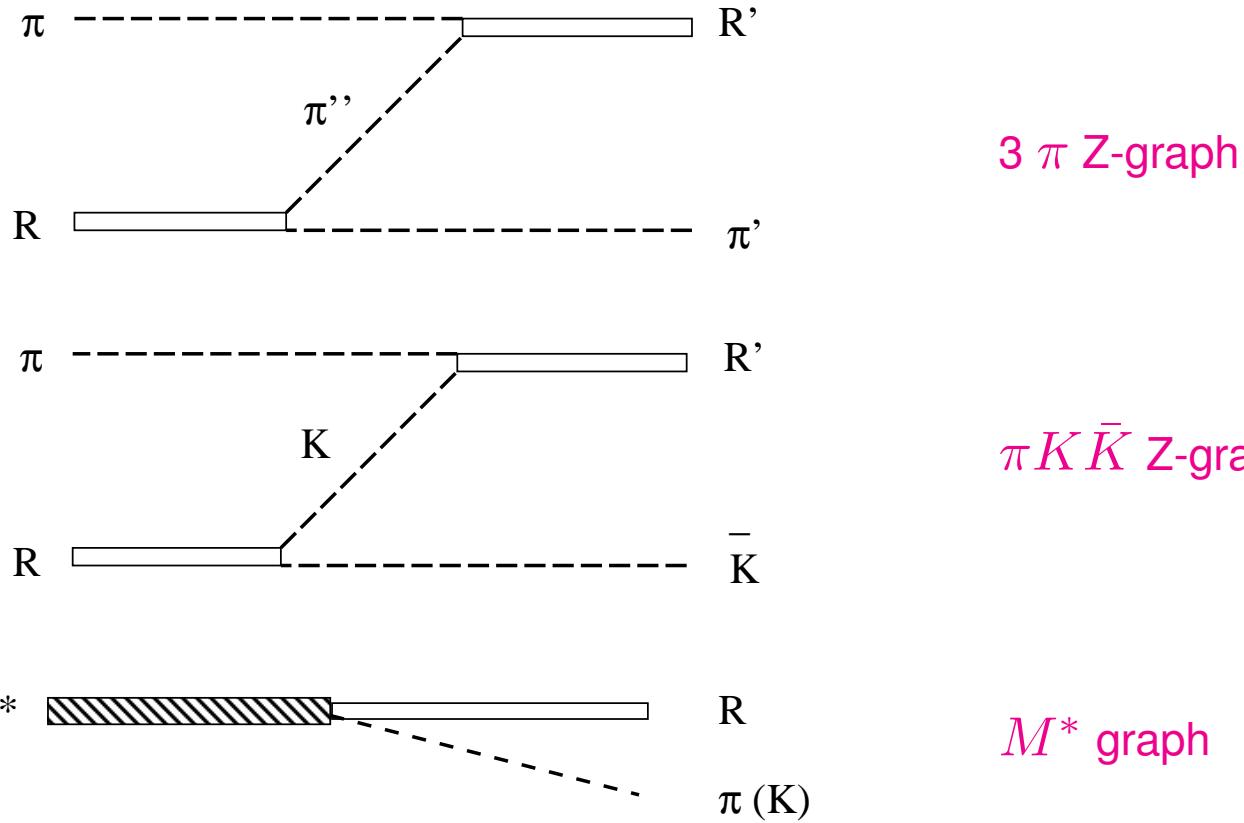


[Data: D. Aston et al. (LASS), NPB **296**, 493 (1988)]

Pole positions in πK amplitude

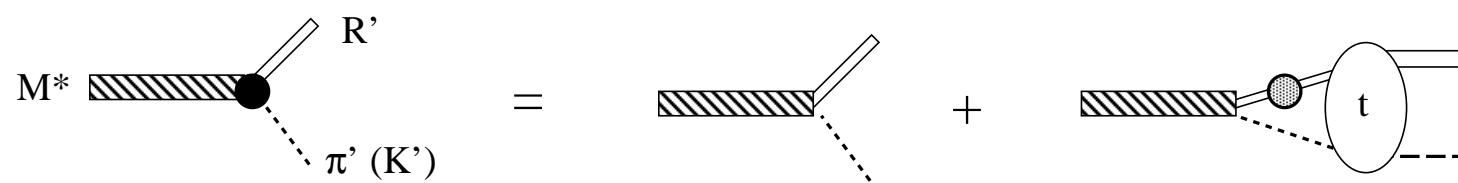
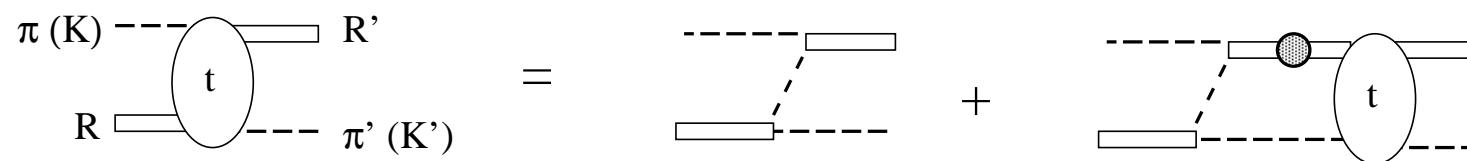
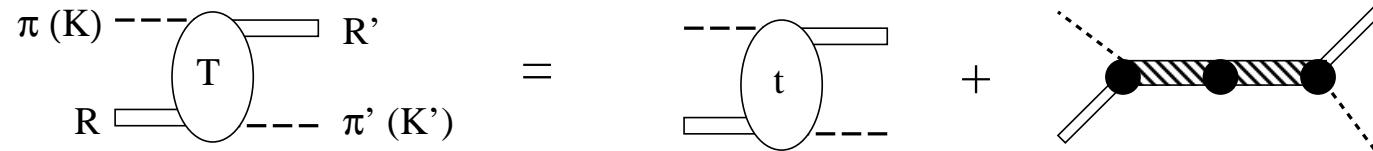
	$\text{Re}[M_R]$ (MeV)		$-\text{Im}[M_R]$ (MeV)	
	Ours	PDG	Ours	PDG
K_0^* (800) (κ)	643	672 ± 40	238	275 ± 17
K_0^* (1430)	1422	1425 ± 50	168	185 ± 40
K^* (892)	901	891.7 ± 0.3	29	25.4 ± 0.5
K^* (1680)	1694	1717 ± 27	152	161 ± 55

Quasi two-particle ($\pi R_{\pi\pi}, \bar{K} R_{\pi K}$) interaction



Z-graphs play an essential role to maintain the 3-body unitarity !

Quasi two-particle ($\pi R_{\pi\pi}, \bar{K} R_{\pi K}$) scattering equation



Application

Effect of Z-graphs (unitarity) on $\pi_2(1670)$ and $\pi_2(2100)$ poles

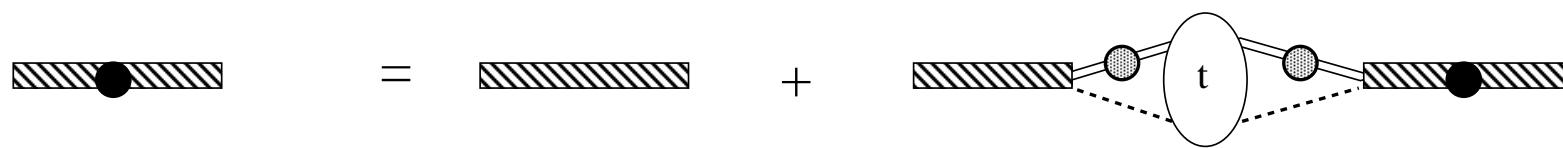
M^*	$\pi_2(1670)$	$\pi_2(2100)$
J^{PC}	2 ⁻⁺	2 ⁻⁺
M_R	$1672 - 130i$ MeV	$2090 - 313i$ MeV
M^*	56 %	35%
$\rightarrow \pi f_2(1270)$	31 %	19 %
$\rightarrow \pi \rho(760)$	11 %	45%
$\rightarrow \pi f_0(600)$		

(Data from PDG)

Fit $M_{\pi_2}^0, g_{\pi_2 \rightarrow \pi R}$ to the pole and branching ratios for $\pi_2(1670), \pi_2(2100)$

Pole search method : Analytic continuation of T-matrix to the unphysical Riemann sheet

Suzuki, Sato, Lee, PRC **79**, 025205 (2009); ibid, **82**, 045206 (2010)



Resonance pole : $W - M_{M^*}^0 - \Sigma_{M^*}(W) = 0$

Fit $M_{\pi_2}^0$, $g_{\pi_2 \rightarrow \pi R}$ to the pole and branching ratios for $\pi_2(1670)$, $\pi_2(2100)$

Pole search method : Analytic continuation of T-matrix to the unphysical Riemann sheet

Suzuki, Sato, Lee, PRC **79**, 025205 (2009); ibid, **82**, 045206 (2010)

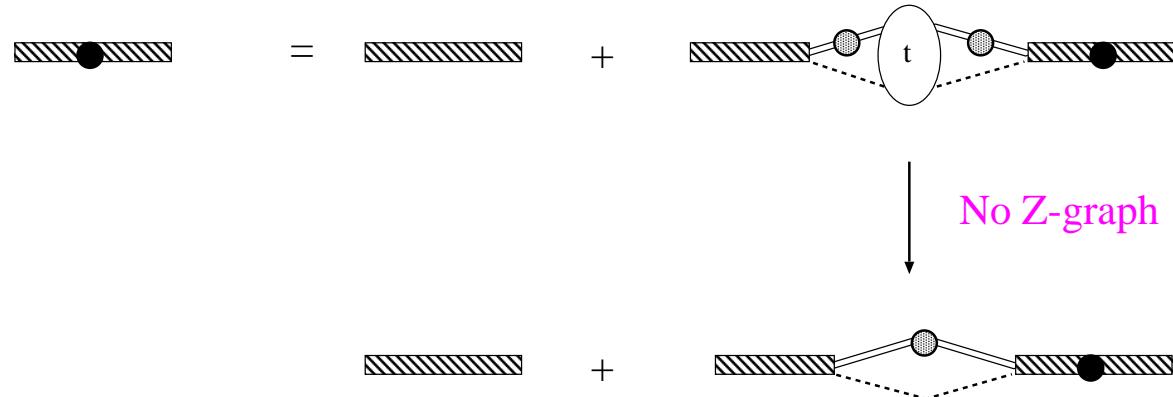
Partial width :

$$\Gamma(\pi_2 \rightarrow \pi R) \equiv -2 \operatorname{Im} \left(g \frac{1}{W - E_\pi - E_R - \Sigma_R} g \right)$$

Branching ratio :

$$B(\pi_2 \rightarrow \pi R) = \frac{\Gamma_R}{\Gamma_{\text{total}}} = \frac{\Gamma_R}{\sum_{R'} \Gamma_{R'}}$$

Effect of Z-graph on the π_2 pole position



Effect of Z-graph on the π_2 pole position



↓
No Z-graph



$\pi_2(1670)$

$\pi_2(2100)$

w Z-graph $1672 - 130 i$ MeV $2090 - 313 i$ MeV

w/o Z-graph $1689 - 133 i$ MeV $2084 - 346 i$ MeV

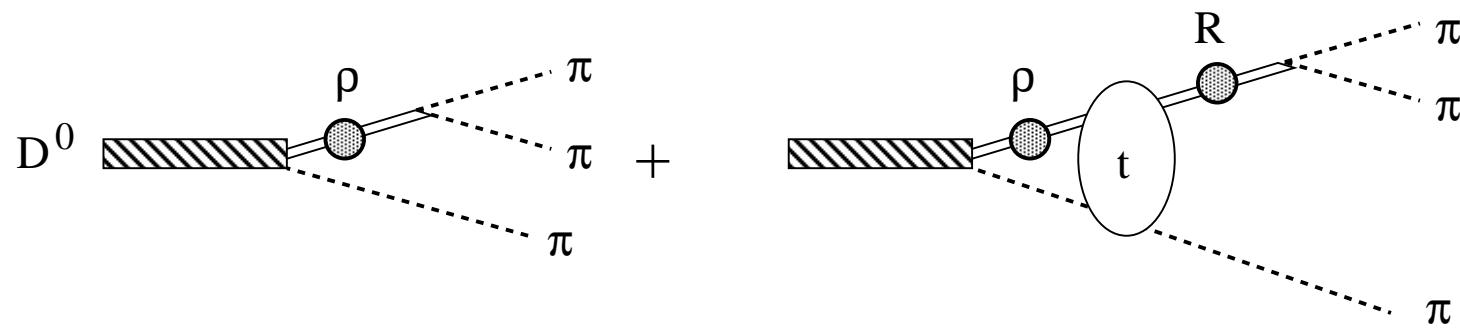
* Z-graph effect on pole position is $\sim 10\%$ for $\pi_2(2100)$ ($\sim 3\%$ for $\pi_2(1670)$)

* $\pi K \bar{K}$ Z-graph has negligible effect

Effect of Z-graphs (unitarity) on Dalitz plot (3 π Z-graph only, no fit, **preliminary**)

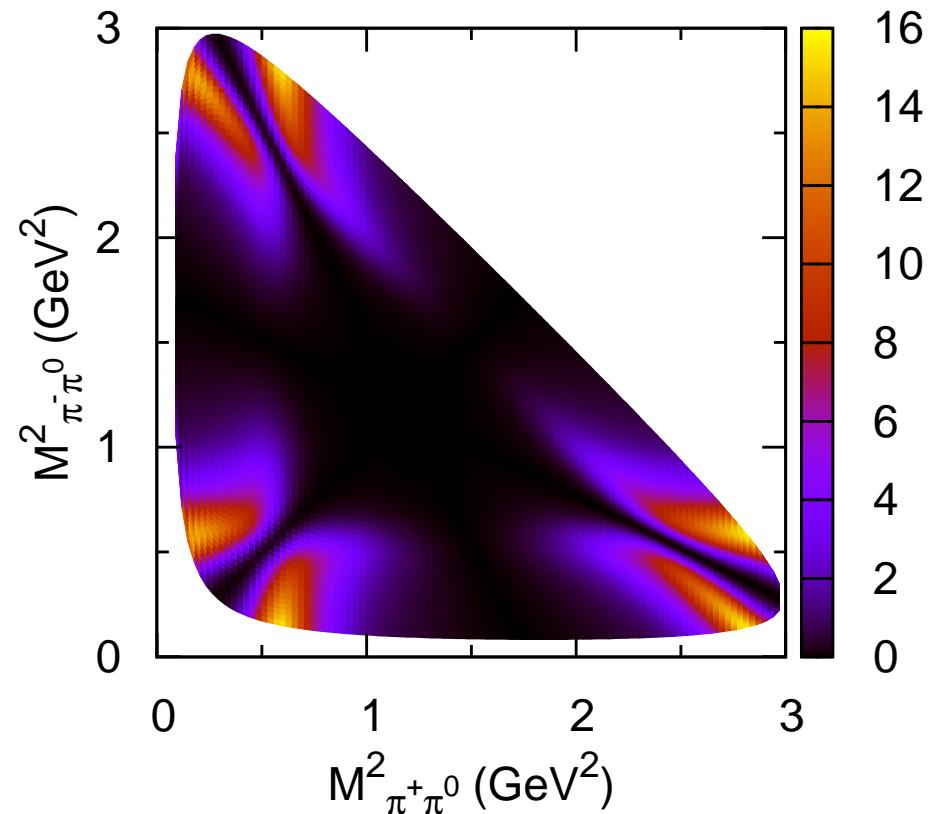
D^0 decay : $D^0 (I = 1/2, J^P = 0^-) \rightarrow \rho\pi (I = 0) \rightarrow \pi^+\pi^-\pi^0$

Decay amplitude



Effect of Z-graphs (unitarity) on Dalitz plot (3 π Z-graph only, no fit, **preliminary**)

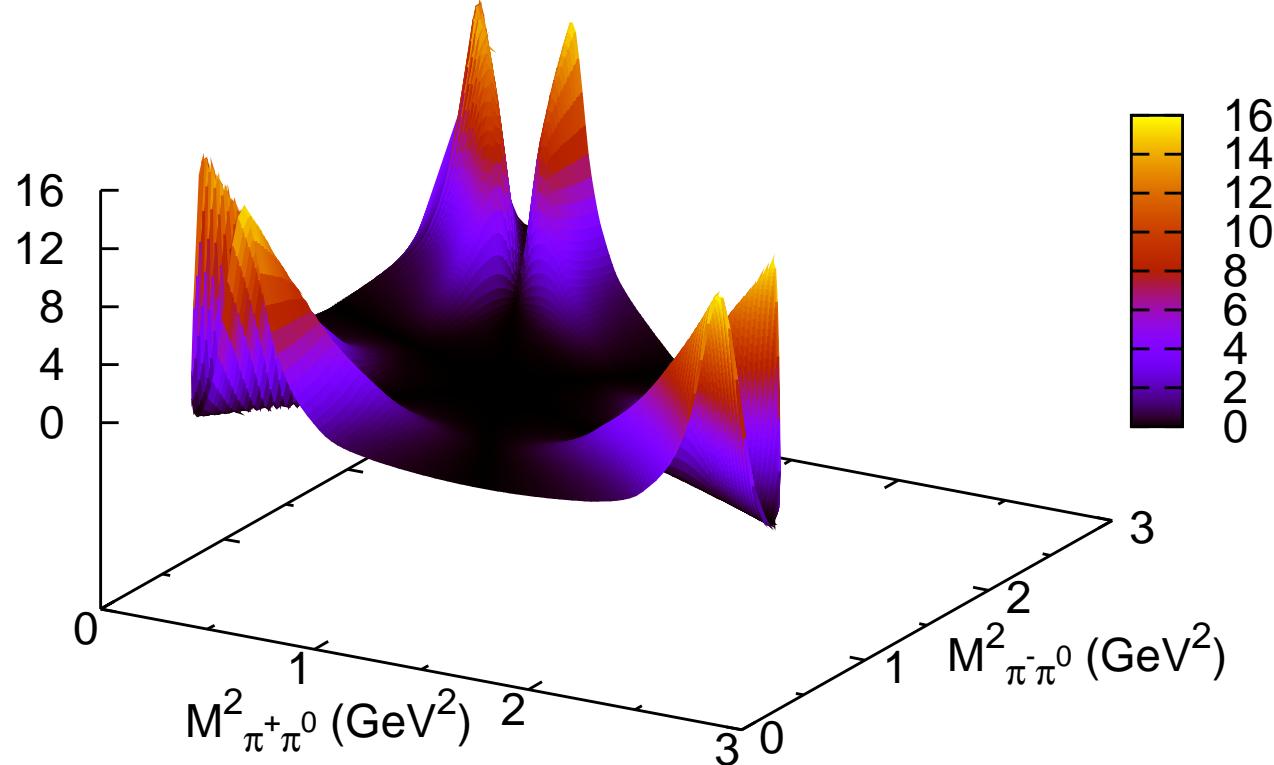
D^0 decay : $D^0 (I = 1/2) \rightarrow \rho\pi (I = 0) \rightarrow \pi^+\pi^-\pi^0$



cf. BABAR, arXiv:1001.3317

Effect of Z-graphs (unitarity) on Dalitz plot (3 π Z-graph only, no fit, **preliminary**)

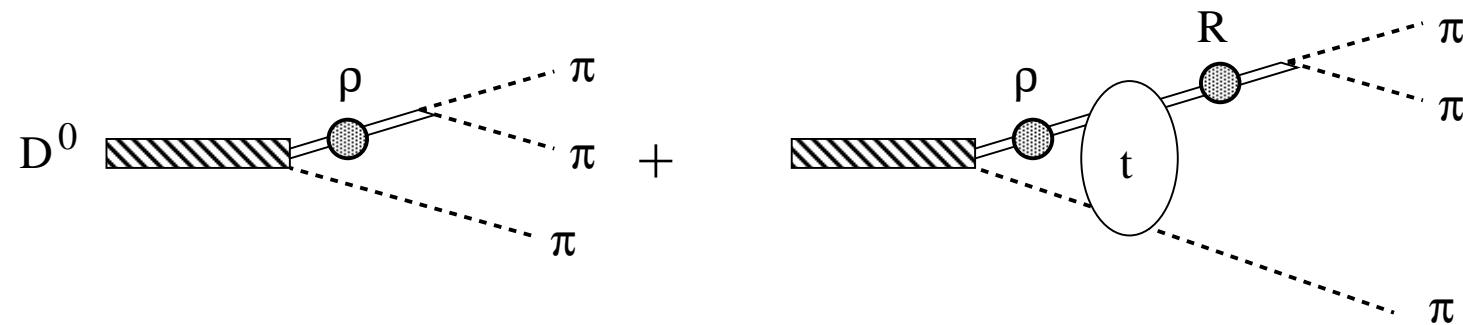
D^0 decay : $D^0 (I = 1/2) \rightarrow \rho\pi (I = 0) \rightarrow \pi^+\pi^-\pi^0$



cf. BABAR, arXiv:1001.3317

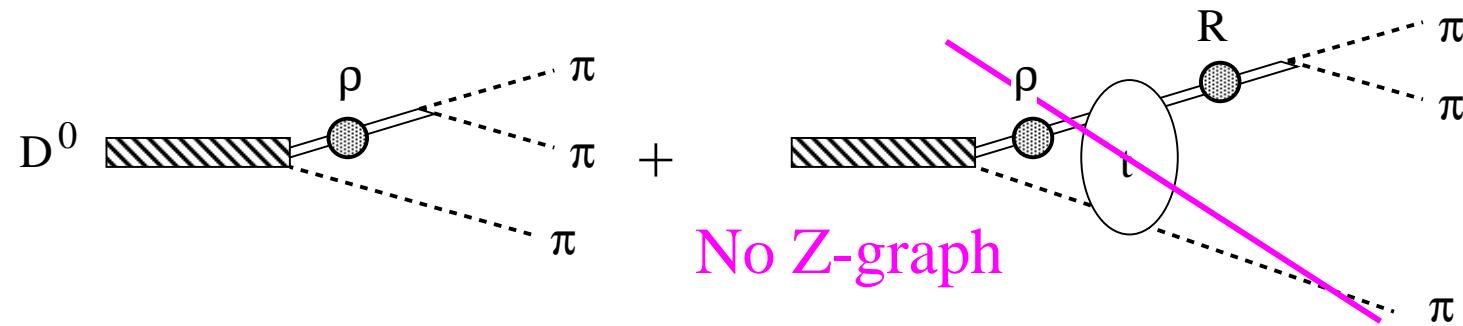
Effect of Z-graphs (unitarity) on Dalitz plot

D⁰ decay : $D^0 (I = 1/2) \rightarrow \rho\pi (I = 0) \rightarrow \pi^+\pi^-\pi^0$



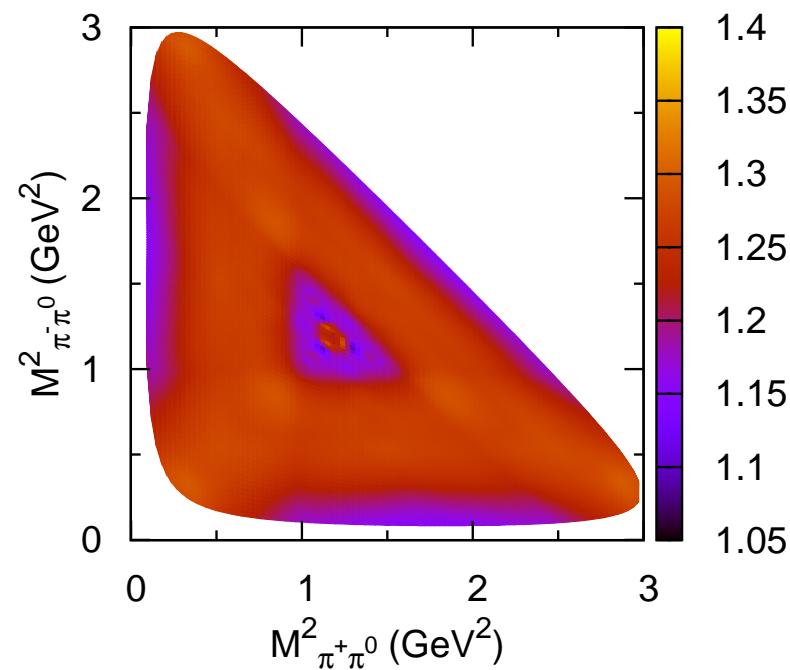
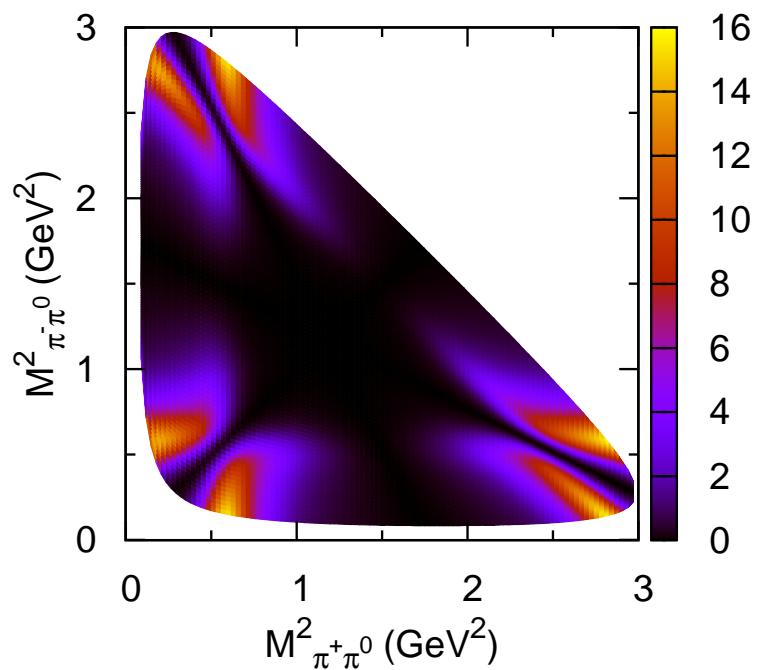
Effect of Z-graphs (unitarity) on Dalitz plot

D⁰ decay : $D^0 (I = 1/2) \rightarrow \rho\pi (I = 0) \rightarrow \pi^+\pi^-\pi^0$



Effect of Z-graphs (unitarity) on Dalitz plot

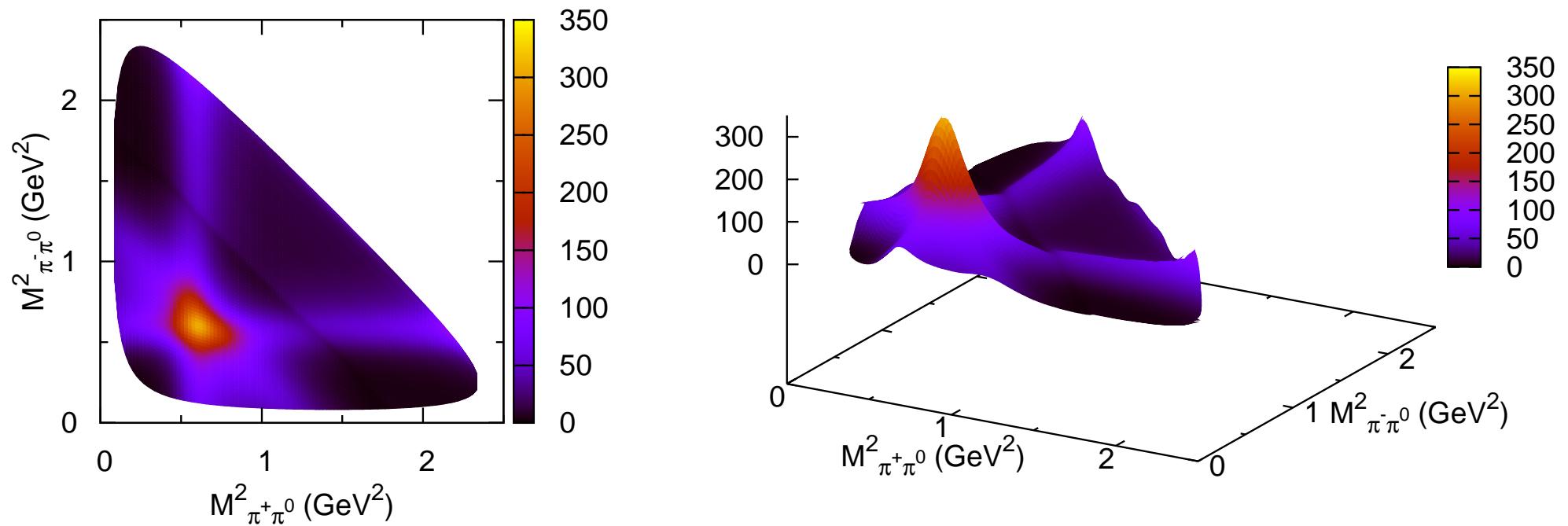
Ratio of Dalitz plots with and w/o Z-graph



Z-graphs (3π unitarity) significantly change magnitude and shape of Dalitz plot !

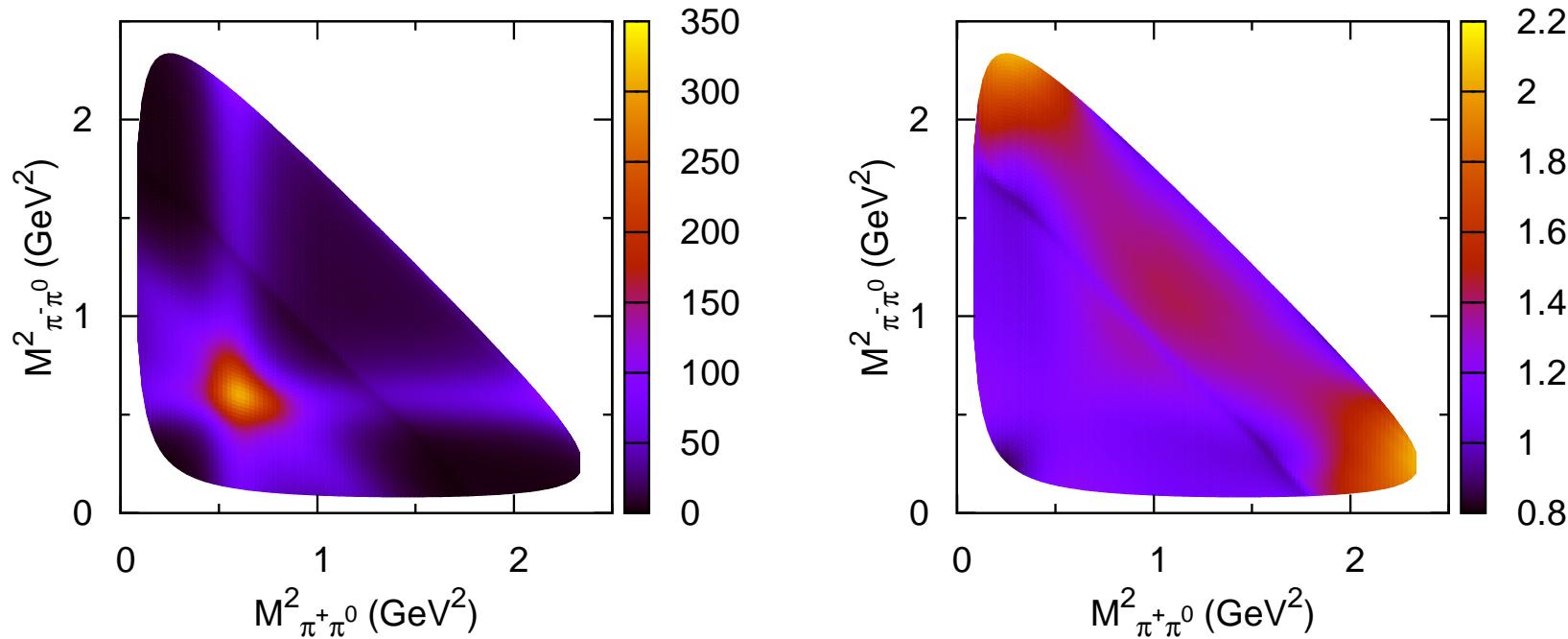
More on Effect of Z-graphs (unitarity) on Dalitz plot

$\pi_2(1670)$ decay : $\pi_2 (I = 1) \rightarrow R\pi (I = 1) \rightarrow \pi^+ \pi^- \pi^0$



More on Effect of Z-graphs (unitarity) on Dalitz plot

$\pi_2(1670)$ decay : Ratio of Dalitz plot with and w/o Z-graphs

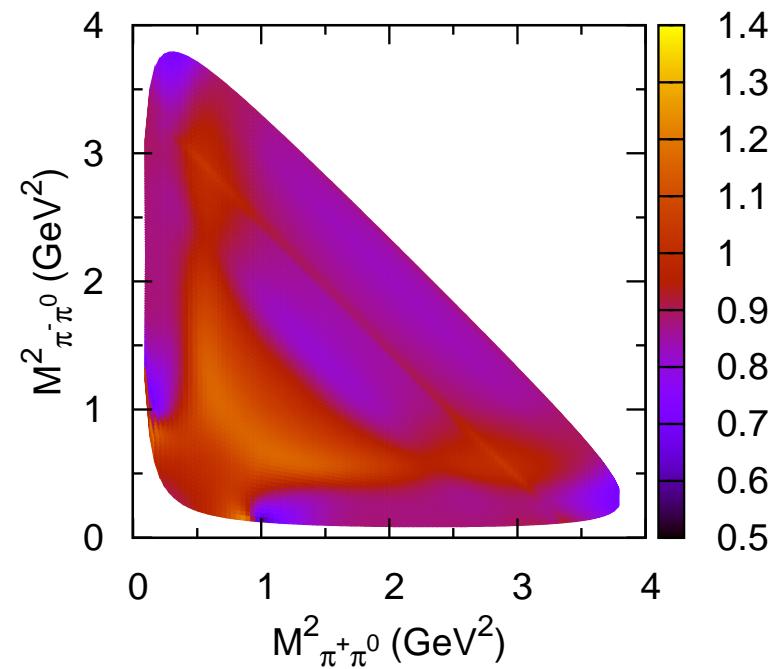
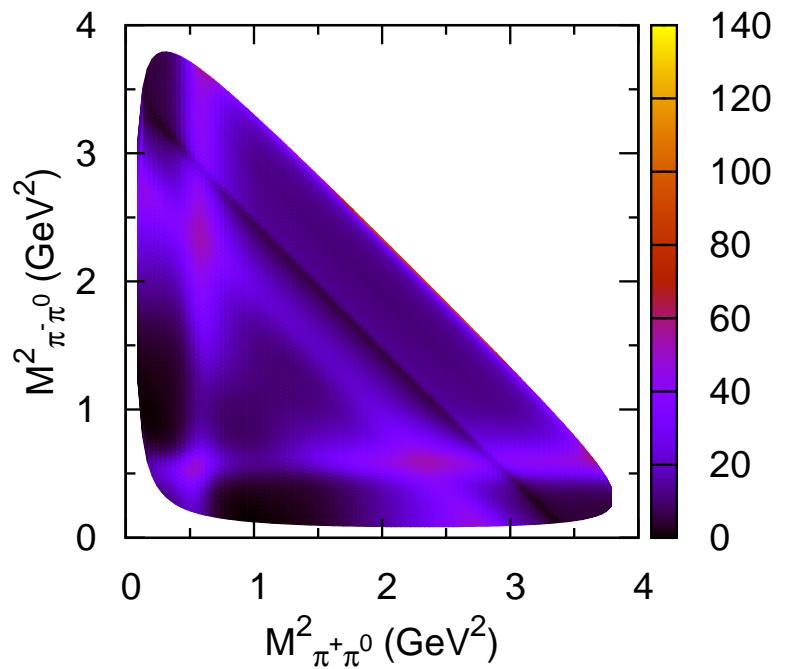


* $\pi_2(1670)$ pole position is rather insensitive to Z-graphs (2-3%)

* Effect of Z-graphs is more visible in Dalitz plot

More on Effect of Z-graphs (unitarity) on Dalitz plot

$\pi_2(2100)$ decay : Ratio of Dalitz plot with and w/o Z-graphs



- * $\pi_2(2100)$ pole position is somewhat sensitive to Z-graphs ($\sim 10\%$)
- * Effect of Z-graphs is even more visible in Dalitz plot

Summary

$3\pi (\pi\pi K)$ from heavy meson decay contains information of interesting physics !

exotic (hybrid) meson, light scalar mesons, CP violation

EBAC (\rightarrow EHAC?) steps toward developing reliable 3π model !

Coupled-channels quasi two-body $(\pi R, KR)$ scattering model

- * $\pi\pi$ and πK models
- * 3π Z-graph, $\pi K \bar{K}$ Z-graph (essential for 3-body unitarity)
- * Bare resonance (M^*) mechanism

Effect of 3π unitarity (Z-graphs) on resonance pole

- * Simple $\pi\pi$ and πK models
- * π_2 (1670), π_2 (2100) ; poles and branching ratios are fitted
- * $\sim 10\%$ (2–3%) shift of the pole due to Z-graph for π_2 (2100) (π_2 (1670))

Effect of 3π unitarity (Z-graphs) on Dalitz plot (preliminary)

- * Generally, Z-graphs change both magnitude and shape of Dalitz plot
- * D^0 decay Dalitz plot is considerably changed (30-40%)
- * Z-graphs effect is more visible in π_2 decay Dalitz plot than pole position